

Appendix D. KSA Exclusions

Findings presented for both mathematics and reading content areas across all occupational areas (CSS, HVAC, LPN, PT Introductory, PT Concluding, and AMT)

NOTES:

The number indicates how many instances across all reviewed packets that the reviewer excluded text in column E. For example, Reviewer 1 in CSS excluded exponents and logarithms in one course out of the total courses reviewed. An exclusion had to be noted three or more times to be noted in the spreadsheet.

NAEP Framework			CSS	HVAC	LPN	PT-Introductory	PT-Concluding	
Measurement in triangles	Interpret and use the identity $\sin^2 \theta + \cos^2 \theta = 1$ for angles θ between 0° and 90° ; recognize this identity as a special representation of the Pythagorean theorem.	2-3-d						
	Determine the radian measure of an angle and explain how radian measurement is related to a circle of radius 1.	2-3-e						
	Use trigonometric formulas such as addition and double angle formulas.	2-3-f						
	Use the law of cosines and the law of sines to find unknown sides and angles of a triangle.	2-3-g						
Dimension and shape	Give precise mathematical descriptions or definitions of geometric shapes in the plane and in three-dimensional space.	3-1-c						
	Draw or sketch from a written description plane figures and planar images of three-dimensional figures.	3-1-d						
	Use two-dimensional representations of three-dimensional objects to visualize and solve problems.	3-1-e						
Transformation of shapes and preservation of properties	Analyze properties of three-dimensional figures including spheres and hemispheres.	3-1-f						
	Recognize or identify types of symmetries (e.g., point, line, rotational, self-congruence) of two- and three-dimensional figures.	3-2-a						
	Give or recognize the precise mathematical relationship (e.g., congruence, similarity, orientation) between a figure and its image under a transformation.	3-2-b						
	Perform or describe the effect of a single transformation on two- and three-dimensional geometric shapes (reflections across lines of symmetry, rotations, translations, and dilations).	3-2-c						
	Identify transformations, combinations, or subdivisions of shapes that preserve the area of two-dimensional figures or the volume of three-dimensional figures.	3-2-d						
	Justify relationships of congruence and similarity and apply these relationships using scaling and proportional reasoning.	3-2-e						
Relationships between geometric figures	Perform or describe the effects of successive transformations.	3-2-g						
	Apply geometric properties and relationships to solve problems in two and three dimensions.	3-3-b	three dimensions	1	1	1	1	
	Represent problem situations with geometric models to solve mathematical or real-world problems.	3-3-c						
	Use the Pythagorean theorem to solve problems in two- or three-dimensional situations.	3-3-d						
	Recall and interpret definitions and basic properties of congruent and similar triangles, circles, quadrilaterals, polygons, parallel, perpendicular and intersecting lines, and associated angle relationships.	3-3-e	lines		1	1		
	Analyze properties or relationships of triangles, quadrilaterals, and other polygonal plane figures.	3-3-f						
	Analyze properties and relationships of parallel, perpendicular, or intersecting lines including the angle relationships that arise in these cases.	3-3-g						
	Analyze properties of circles and the intersections of lines and circles (inscribed angles, central angles, tangents, secants, and chords).	3-3-h						
	Solve problems involving the coordinate plane such as the distance between two points, the midpoint of a segment, or slopes of perpendicular or parallel lines.	3-4-a						
	Describe the intersections of lines in the plane and in space, intersections of a line and a plane, or of two planes in space.	3-4-b						
Position, direction, and coordinate geometry	Describe or identify conic sections and other cross sections of solids.	3-4-c						
	Represent two-dimensional figures algebraically using coordinates and/or equations.	3-4-d						
	Use vectors to represent velocity and direction; multiply a vector by a scalar and add vectors both algebraically and graphically.	3-4-e						
	Find an equation of a circle given its center and radius and, given an equation of a circle, find its center and radius.	3-4-f						
	Graph ellipses and hyperbolas whose axes are parallel to the coordinate axes and demonstrate understanding of the relationship between their standard algebraic form and their graphical characteristics.	3-4-g						
	Represent situations and solve problems involving polar coordinates.	3-4-h						
	Mathematical reasoning in geometry	Make, test, and validate geometric conjectures using a variety of methods including deductive reasoning and counter examples.	3-5-a					
		Determine the role of hypotheses, logical implications, and conclusion in proofs of geometric theorems.	3-5-b					
Analyze or explain a geometric argument by contradiction.		3-5-c						
Analyze or explain a geometric proof of the Pythagorean theorem.		3-5-d						
Prove basic theorems about congruent and similar triangles and circles.		3-5-e						
Read or interpret graphical or tabular representations of data.	4-1-a	graphical				2	1	

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Data representation	For a given set of data, complete a graph and solve a problem using the data in the graph (histograms, scatterplots, and line graphs).	4-1-b					
	Solve problems involving univariate or bivariate data.	4-1-c	bivariate data	5			
	Given a graphical or tabular representation of a set of data, determine whether information is represented effectively and appropriately.	4-1-d					
	Compare and contrast different graphical representations of univariate and bivariate data.	4-1-e					
	Organize and display data in a spreadsheet in order to recognize patterns and solve problems.	4-1-f	display data in a spreadsheet	4			
	Characteristics of data sets	Calculate, interpret, or use summary statistics for distributions of data including measures of typical value (mean, median), position (quartiles, percentiles), and spread (range, interquartile range, variance, and standard deviation).	4-2-a				
Recognize how linear transformations of one-variable data affect mean, median, mode, range, interquartile range, and standard deviation.		4-2-b					
Determine the effect of outliers on mean, median, mode, range, interquartile range, or standard deviation.		4-2-c					
Compare data sets using summary statistics (mean, median, mode, range, interquartile range, or standard deviation) describing the same characteristic for two different populations or subsets of the same population.		4-2-d					
Approximate a trend line if a linear pattern is apparent in a scatterplot or use a graphing calculator to determine a least squares regression line and use the line or equation to make predictions.		4-2-e					
Recognize that the correlation coefficient is a number from -1 to +1 that measures the strength of the linear relationship between two variables; visually estimate the correlation coefficient (e.g., positive or negative, closer to 0, .5, or 1.0) of a scatterplot.		4-2-f					
Know and interpret the key characteristics of a normal distribution such as shape, center (mean), and spread (standard deviation).		4-2-g					
Experiments and samples	Identify possible sources of bias in sample surveys and describe how such bias can be controlled and reduced.	4-3-a					
	Recognize and describe a method to select a simple random sample.	4-3-b					
	Draw inferences from samples, such as estimates of proportions in a population, estimates of population means, or decisions about differences in means for two "treatments."	4-3-c					
	Identify or evaluate the characteristics of a good survey or of a well-designed experiment.	4-3-d					
	Recognize the differences in design and in conclusions between randomized experiments and observational studies.	4-3-e					
Probability	Recognize whether two events are independent or dependent.	4-4-a					
	Determine the theoretical probability of simple and compound events in familiar or unfamiliar contexts.	4-4-b					
	Given the results of an experiment or simulation, estimate the probability of simple or compound events in familiar or unfamiliar contexts.	4-4-c					
	Use theoretical probability to evaluate or predict experimental outcomes.	4-4-d					
	Determine the number of ways an event can occur using tree diagrams, formulas for combinations and permutations, or other counting techniques.	4-4-e					
	Determine the probability of independent and dependent events.	4-4-h					
	Determine conditional probability using two-way tables.	4-4-i					
Mathematical reasoning with data	Interpret and apply probability concepts to practical situations.	4-4-j					
	Use the binomial theorem to solve problems.	4-4-k					
	Identify misleading uses of data in real-world settings and critique different ways of presenting and using information.	4-5-a					
	Distinguish relevant from irrelevant information, identify missing information, and either find what is needed or make appropriate approximations.	4-5-b	reasoning not related to mathematical issues	3	8		
	Recognize, use, and distinguish between the processes of mathematical (deterministic) and statistical modeling.	4-5-c					
	Recognize when arguments based on data confuse correlation with causation.	4-5-d					
Patterns	Recognize and explain the potential errors caused by extrapolating from data.	4-5-e					
	Recognize, describe, or extend numerical patterns, including arithmetic and geometric progressions.	5-1-a					
	Express linear and exponential functions in recursive and explicit form given a table, verbal description, or some terms of a sequence.	5-1-b	exponential functions	2	1		
	Identify or analyze distinguishing properties of linear, quadratic, rational, exponential, or *trigonometric functions from tables, graphs, or equations.	5-1-e	trigonometric		1	1	1
Determine whether a relation, given in verbal, symbolic, tabular, or graphical form, is a function.	5-1-g						

